## Chapter 5

## Decision-Making under <br> Uncertain Conditions

# Operations Management 

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## Agenda

> Newsvendor Problem
> Newsvendor Example
$>$ Procurement Contracts
$>$ Decision Challenge
$>$ Decision Biases

## Newsvendor Model

Businesses which are based on ordering seasonal or perishable products:

- Newspaper vendors (daily)
- Fashion (couple of months)
- Ski equipment retailers (annually, before ski season)
- Halloween custom sellers (annually, before Halloween)
- Dairy product sellers (couple of days or weeks)
- ...

Demand is uncertain and materialize after you receive the product

## Newsvendor Model

The challenge of finding the best order size:

- Order size smaller than demand: lost sales (underage cost)
- Order size larger than demand: excess inventor (overage cost)

What is the optimal order size which balances these two costs?

## Newsvendor Model

Unit cost $=c$
Selling price $=p$

- Overage Cost $=C_{o}=c-s$

Salvage price $=s$

- Underage cost $=C_{u}=p-c$

Demand $=D$ (random)
Order size $=Q$

- Optimal Order Quantity $=Q^{*}$

$$
\operatorname{Pr}\left(D \leq Q^{*}\right)=F\left(Q^{*}\right)=\frac{C_{u}}{C_{u}+C_{o}}=\frac{p-c}{p-s}
$$

- Uniform Demand Distribution: $D \sim \mathrm{U}(a, b)$

$$
Q^{*}=\frac{C_{u}}{C_{u}+C_{o}}(b-a)+a
$$

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## Newsvendor Example

Average Demand: 200
100< Demand < 300


$$
\begin{aligned}
& \begin{aligned}
& \qquad \begin{aligned}
\text { Overage Cost }=\mathrm{Co} & =17 \\
\text { Underage Cost }=\mathrm{Cu} & =20-17=3 \\
\text { (Uniform Dist.) } & \mathrm{a}
\end{aligned} \mathrm{=100} \\
& \text { (Uniform Dist.) } \mathrm{b}
\end{aligned}=300 \\
& 3 \\
& Q^{*}=\frac{3}{17+3} \times 200+100=130
\end{aligned}
$$

## Newsvendor Model Example

The commute time from your home to your work is a random variable. It is never less than 20 minutes and in the worst traffic it takes 40 minutes for you to get to work. Your experience tells you the commute time is (approximately) uniformly distributed between these to extremes.
Getting to your work earlier than work hours is a waste of time. Getting to work late creates a bad image for you in the work place. So, both being late and being early creates a level discomfort for you. If you are asked to give weights to the level of discomfort from being early or late (on a scale of 1 to 10), you give a weight of 3 for every minute of being early and a weight of 9 for every minute of being late. How many minutes before the start of work hours should you leave your home to minimize your discomfort in this regard?

## Newsvendor Model Example

$$
\begin{aligned}
& \qquad \begin{aligned}
\text { Overage Cost }=\mathrm{Co} & =3 \\
\text { Underage Cost }=\mathrm{Cu} & =9 \\
\text { (Uniform Dist.) } & \mathrm{a}
\end{aligned}=20 \\
& \text { (Uniform Dist.) } \mathrm{b}
\end{aligned}=40
$$

$$
Q^{*}=\frac{C_{u}}{C_{u}+C_{o}}(b-a)+a=\frac{9}{9+3}(40-20)+20=35 \mathrm{~min}
$$

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## Wholesales Price Contract



## What is wrong with this type of contract?

The retailer bears all the risk and therefore, to avoid overage cost, orders less than what is best for the whole chain.

## Revenue Sharing Contract



## The supplier shares the risk?

If the "Revenue Sharing Price" and the "Shared Revenue" are set to the right value, the retailer order enough items to maximize the profit of the whole chain.

## Buyback Contract



## The supplier shares the risk?

If the "Buyback Price" and the "Unsold Item Price" are set to the right value, the retailer order enough items to maximize the profit of the whole chain.

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## Wholesale Contract

Average Demand: 200
100< Demand < 300


## Demand Distribution

$\checkmark$ Uniform Demand Distribution $\sim(100,300)$


## Revenue Sharing Contract



Demand $>$ Order Quantity $\rightarrow$ You lose $\$ 4$ for any unsatisfied demand $(\$ 4=\$ 20-\$ 1-\$ 15)$
Order Quantity> Demand $\rightarrow$ You lose \$1 for any unsold product

Demand > Order Quantity
Order Quantity = 200 units
Realized Demand= 250 units

You loose the opportunity to sell: $\mathbf{( 2 5 0 - 2 0 0})=\mathbf{5 0}$ units

Lost SALES opportunity: 50*\$4=\$200!

Order Quantity> Demand

- Order Quantity = 200 units
- Realized Demand= 150 units
- Unsold Items: (200-150)=50 units
- Cost of Unsold Items: 50*\$1=\$50!


## Do the Decision Practice in Excel File

Watch the video for Decision Practice

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## Decision Practice Results



## Decision Competition Results



This is Called Pull to Center Effect

